

$$\begin{aligned}
&> \text{restart} \\
&> \text{Ecua} := 4 \cdot x^2 - x \cdot y + y^2 + (x^2 - x \cdot y + 4 \cdot y^2) \cdot y' = 0 \\
&\quad \text{Ecua} := 4 x^2 - x y(x) + y(x)^2 + (x^2 - x y(x) + 4 y(x)^2) \left( \frac{d}{dx} y(x) \right) = 0 \tag{1} \\
&> \text{with(DEtools)} : \\
&> \text{odeadvisor}(\text{Ecua}) \\
&\quad [[_{\text{homogeneous}}, \text{class } A], _{\text{rational}}, _{\text{dAlembert}}] \tag{2} \\
&> \text{EcuaDos} := \text{simplify}(\text{isolate}(\text{eval}(\text{subs}(y(x) = u(x) \cdot x, \text{Ecua})), \text{diff}(u(x), x))) \\
&\quad \text{EcuaDos} := \frac{d}{dx} u(x) = \frac{-4 u(x)^3 - 4}{x (4 u(x)^2 - u(x) + 1)} \tag{3} \\
&> \text{odeadvisor}(\text{EcuaDos}) \\
&\quad [_{\text{separable}}] \tag{4} \\
&> M := -(-4 u^3 - 4) \\
&\quad M := 4 u^3 + 4 \tag{5} \\
&> N := x (4 u^2 - u + 1) \\
&\quad N := x (4 u^2 - u + 1) \tag{6} \\
&> Px := 4; Qu := u^3 + 1; Rx := x; Su := 4 \cdot u^2 - u + 1 \\
&\quad Px := 4 \\
&\quad Qu := u^3 + 1 \\
&\quad Rx := x \\
&\quad Su := 4 u^2 - u + 1 \tag{7} \\
&> \text{SolGralCero} := \text{int}\left(\frac{Px}{Rx}, x\right) + \text{int}\left(\frac{Su}{Qu}, u\right) = \_C1 \\
&\quad \text{SolGralCero} := 4 \ln(x) + 2 \ln(u + 1) + \ln(u^2 - u + 1) = \_C1 \tag{8} \\
&> \text{SolGralUno} := \text{subs}\left(u = \frac{y(x)}{x}, \text{SolGralCero}\right) \\
&\quad \text{SolGralUno} := 4 \ln(x) + 2 \ln\left(\frac{y(x)}{x} + 1\right) + \ln\left(\frac{y(x)^2}{x^2} - \frac{y(x)}{x} + 1\right) = \_C1 \tag{9} \\
&> \text{SolGralFinal} := \text{expand}(\text{simplify}(\text{exp}(\text{lhs}(\text{SolGralUno}))) = \_C10) \\
&\quad \text{SolGralFinal} := y(x)^4 + y(x)^3 x + x^3 y(x) + x^4 = \_C10 \tag{10} \\
&> \text{Ecua} \\
&\quad 4 x^2 - x y(x) + y(x)^2 + (x^2 - x y(x) + 4 y(x)^2) \left( \frac{d}{dx} y(x) \right) = 0 \tag{11} \\
&> \text{DerSolFinal} := \text{isolate}(\text{diff}(\text{SolGralFinal}, x), \text{diff}(y(x), x)) \\
&\quad \text{DerSolFinal} := \frac{d}{dx} y(x) = \frac{-y(x)^3 - 3 y(x) x^2 - 4 x^3}{4 y(x)^3 + 3 y(x)^2 x + x^3} \tag{12} \\
&> \text{DerEcua} := \text{isolate}(\text{Ecua}, \text{diff}(y(x), x)) \tag{13}
\end{aligned}$$

$$DerEcua := \frac{d}{dx} y(x) = \frac{-4x^2 + xy(x) - y(x)^2}{x^2 - xy(x) + 4y(x)^2} \quad (13)$$

$$\begin{aligned} > Comprobar := simplify(rhs(DerEcua) - rhs(DerSolFinal) = 0) \\ Comprobar &:= 0 = 0 \end{aligned} \quad (14)$$

> restart

$$\begin{aligned} > Ecua &:= y' = \frac{2 \cdot x \cdot y}{3x^2 - y^2} \\ Ecua &:= \frac{d}{dx} y(x) = \frac{2xy(x)}{3x^2 - y(x)^2} \end{aligned} \quad (15)$$

> with(DEtools):

$$\begin{aligned} > odeadvisor(Ecua) \\ &[[_homogeneous, class A], _rational, _dAlembert] \end{aligned} \quad (16)$$

$$\begin{aligned} > EcuaDos &:= simplify(isolate(eval(subs(y(x) = x \cdot u(x), Ecua)), diff(u(x), x))) \\ EcuaDos &:= \frac{d}{dx} u(x) = \frac{u(x) \left( -1 + \frac{2}{3 - u(x)^2} \right)}{x} \end{aligned} \quad (17)$$

$$\begin{aligned} > Mxu &:= expand\left(-\left(u \cdot \left(-1 + \frac{2}{3 - u^2}\right)\right)\right) \\ Mxu &:= u - \frac{2u}{-u^2 + 3} \end{aligned} \quad (18)$$

$$\begin{aligned} > Nxu &:= x \\ Nxu &:= x \end{aligned} \quad (19)$$

$$\begin{aligned} > Px &:= 1; Qu := Mxu; Rx := x; Su := 1 \\ Px &:= 1 \\ Qu &:= u - \frac{2u}{-u^2 + 3} \\ Rx &:= x \\ Su &:= 1 \end{aligned} \quad (20)$$

$$\begin{aligned} > SolGralCero &:= int\left(\frac{Px}{Rx}, x\right) + int\left(\frac{Su}{Qu}, u\right) = _CI \\ SolGralCero &:= \ln(x) - \ln(u - 1) - \ln(u + 1) + 3 \ln(u) = _CI \end{aligned} \quad (21)$$

$$\begin{aligned} > SolGralUno &:= subs\left(u = \frac{y(x)}{x}, SolGralCero\right) \\ SolGralUno &:= \ln(x) - \ln\left(\frac{y(x)}{x} - 1\right) - \ln\left(\frac{y(x)}{x} + 1\right) + 3 \ln\left(\frac{y(x)}{x}\right) = _CI \end{aligned} \quad (22)$$

$$\begin{aligned} > SolFinal &:= simplify(exp(lhs(SolGralUno))) = _CI0 \\ SolFinal &:= \frac{y(x)^3}{y(x)^2 - x^2} = _CI0 \end{aligned} \quad (23)$$

> Ecua

$$\frac{d}{dx} y(x) = \frac{2 x y(x)}{3 x^2 - y(x)^2} \quad (24)$$

> *DerSolFinal* := isolate(diff(*SolFinal*, x), diff(y(x), x))

$$\text{DerSolFinal} := \frac{d}{dx} y(x) = -\frac{2 y(x) x}{y(x)^2 - 3 x^2} \quad (25)$$

> restart

> *Ecua* := (2·x·y<sup>3</sup> - 6·y<sup>4</sup> + 12·x<sup>2</sup>·y) + (3·x<sup>2</sup>·y<sup>2</sup> - 24·x·y<sup>3</sup> + 4·x<sup>3</sup> + 4·y) · y' = 0

$$\text{Ecua} := 2 x y(x)^3 - 6 y(x)^4 + 12 x^2 y(x) + (3 x^2 y(x)^2 - 24 x y(x)^3 + 4 x^3 + 4 y(x)) \left( \frac{d}{dx} y(x) \right) = 0 \quad (26)$$

> with(DEtools) :

> odeadvisor(*Ecua*)

[\_exact, \_rational] (27)

> *Mxy* := 2 x y<sup>3</sup> - 6 y<sup>4</sup> + 12 x<sup>2</sup> y

$$\text{Mxy} := 2 x y^3 - 6 y^4 + 12 x^2 y \quad (28)$$

> *Nxy* := (3 x<sup>2</sup> y<sup>2</sup> - 24 x y<sup>3</sup> + 4 x<sup>3</sup> + 4 y)

$$\text{Nxy} := 3 x^2 y^2 - 24 x y^3 + 4 x^3 + 4 y \quad (29)$$

> *IntMx* := simplify(int(*Mxy*, x))

$$\text{IntMx} := x^2 y^3 - 6 x y^4 + 4 x^3 y \quad (30)$$

> *SolGralUno* := *IntMx* + int((*Nxy* - diff(*IntMx*, y)), y) = \_C1

$$\text{SolGralUno} := x^2 y^3 - 6 x y^4 + 4 x^3 y + 2 y^2 = \_C1 \quad (31)$$

> *IntNy* := int(*Nxy*, y)

$$\text{IntNy} := x^2 y^3 - 6 x y^4 + 4 x^3 y + 2 y^2 \quad (32)$$

> *SolGralDos* := *IntNy* + int((*Mxy* - diff(*IntNy*, x)), x) = C1

$$\text{SolGralDos} := x^2 y^3 - 6 x y^4 + 4 x^3 y + 2 y^2 = C1 \quad (33)$$

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